

Home Search Collections Journals About Contact us My IOPscience

Constraining the MSSM with universal gaugino masses and implication for searches at the LHC

This article has been downloaded from IOPscience. Please scroll down to see the full text article.

JHEP11(2009)026

(http://iopscience.iop.org/1126-6708/2009/11/026)

The Table of Contents and more related content is available

Download details: IP Address: 80.92.225.132 The article was downloaded on 01/04/2010 at 13:33

Please note that terms and conditions apply.

PUBLISHED BY IOP PUBLISHING FOR SISSA

RECEIVED: July 16, 2009 REVISED: October 6, 2009 ACCEPTED: October 19, 2009 PUBLISHED: November 6, 2009

# Constraining the MSSM with universal gaugino masses and implication for searches at the LHC

G. Bélanger,<sup>a</sup> F. Boudjema,<sup>a</sup> A. Pukhov<sup>b</sup> and R.K. Singh<sup>a,c</sup>
<sup>a</sup>LAPTH, Univ. de Savoie, CNRS, B.P.110, F-74941 Annecy-le-Vieux, France

ABSTRACT: Using a Markov chain Monte Carlo approach, we find the allowed parameter space of a MSSM model with seven free parameters. In this model universality conditions at the GUT scale are imposed on the gaugino sector. We require in particular that the relic density of dark matter saturates the value extracted from cosmological measurements assuming a standard cosmological scenario. We characterize the parameter space of the model that satisfies experimental constraints and illustrate the complementarity of the LHC searches, B-physics observables and direct dark matter searches for further probing the parameter space of the model. We also explore the different decay chains expected for the coloured particles that would be produced at LHC.

**KEYWORDS:** Supersymmetry Phenomenology

ARXIV EPRINT: 0906.5048



 <sup>&</sup>lt;sup>b</sup>Skobeltsyn Inst. of Nuclear Physics, Moscow State Univ., Moscow 119992, Russia

<sup>&</sup>lt;sup>c</sup>Institut für Theoretische Physik und Astrophysik, Universität Würzburg, D-97074 Würzburg, Germany

*E-mail:* belanger@lapp.in2p3.fr, boudjema@lapp.in2p3.fr, pukhov@lapp.in2p3.fr, singh@physik.uni-wuerzburg.de

## Contents

1	Introduction	1
<b>2</b>	Model and constraints	4
3	Parameter sampling method	6
4	Results	8
	4.1 The allowed parameter space of the MSSM	9
	4.2 The particle spectrum	11
	4.3 Other observables	13
	4.4 Complementarity of different LHC searches and direct dark matter sear	ches 17
	4.5 Impact of improved sensitivity	21
<b>5</b>	LHC forecasts	22
	5.1 Scenarios where $m_{\tilde{g}} < 2$ TeV, $M_{\tilde{q}} > 2$ TeV	22
	5.2 Scenarios where $M_{\tilde{q}} < 2 \text{ TeV}, m_{\tilde{g}} > 2 \text{ TeV}$	26
	5.3 Scenarios where $M_{\tilde{q}} < 2$ TeV, $m_{\tilde{g}} < 2$ TeV	27
6	Conclusion	28

## 1 Introduction

Among the large number of theoretical models proposed to either solve the hierarchy problem and/or explain dark matter with a new stable particle, the minimal supersymmetric model (MSSM) remains one of the favourite. Supersymmetry not only provides a solution to both these problems but also predicts new physics around the TeV scale. The main drawback of the MSSM apart from the lack of evidence for supersymmetric particles is the large number of unknown parameters most of which describe the symmetry breaking sector. With the improved sensitivities of dark matter searches in astroparticle experiments [1–6], the precise determination of the DM relic density from cosmology [7–9], the latest results from the Tevatron [10, 11] and the precision measurements like *amu*, large regions of the parameter space of the supersymmetric models are being probed. This will continue in the near future with a number of direct and indirect detection experiments improving their sensitivities [12–15] and most importantly with the LHC starting to take data. The LHC running at the full design energy of 14TeV offers good prospects for producing coloured supersymmetric particles lighter than 2-3 TeV, for discovering one or more Higgs scalars [16, 17] and for measuring the rare processes in the flavour sector, in particular in B-physics [18]. Furthermore some properties of the sparticles, in particular mass differences can be measured precisely in some scenarios [16, 17].

The first studies that extracted constraints on supersymmetric models worked in general within the context of the MSSM embedded in a GUT scale model such as the CMSSM [19–21]. After specifying the fundamental model parameters at the high scale, the renormalisation group equations are used to obtain the weak scale particle spectrum. This approach provides a convenient framework for phenomenological analyses as the number of free parameters is reduced drastically compared to the general MSSM (from O(100) to 4 and 1/2 parameters in the case of the CMSSM). The drawback is that one is often confined to very specific scenarios, for example in the CMSSM the LSP is dominantly bino over most of the parameter space. This has important consequences for the dark matter relic abundance. Furthermore it was customary to choose some specific values for some of the MSSM or even the SM parameters for a convenient representation of the parameter space in two-dimensions. While the link between specific observables and allowed regions of parameter space is easier to grasp in this framework, the allowed parameter space appeared much more restrictive than if all free parameters were allowed to vary.

In the last few years efficient methods for exploring multi-dimensional parameter space have been used in particle physics and more specifically for determining the allowed parameter space of the CMSSM. This approach showed that the often narrow strips in parameter space obtained when varying only two parameters at a time fattened to large areas [22-25]after letting all parameters of the CMSSM and the SM vary in the full range. With this efficient parameter space sampling method it becomes possible to relax some theoretical assumptions and consider the full parameter space of the MSSM. Because the number of experimental constraints on TeV scale physics is still rather limited it seems a bit premature to go to the full fledge  $\mathcal{O}(100)$  parameters of the MSSM or even to the 19 parameters that characterize the model when assuming no flavour structure and equality of all soft parameters for the first and second generations of sfermions (for an approach along these lines see [26, 27]). Furthermore many parameters, for example those of the first and second generations of squarks, once chosen to be equal to avoid strong flavour-changing neutral current constraints, do not play an important role in the observables selected to fit the model. Here we consider a model where input parameters of the MSSM are defined at the weak scale and we add some simplifying assumptions: common slepton masses  $(M_{\tilde{l}_R} = M_{\tilde{l}_L} = M_{\tilde{l}})$  and common squark masses  $(M_{\tilde{q}_R} = M_{\tilde{q}_L} = M_{\tilde{q}})$  at the weak scale for all three generations and universality of gaugino parameters at the GUT scale. This implies the following relation between the gaugino masses at the weak scale,  $M_2 = 2M_1 = M_3/3$ . We furthermore assume that  $A_t$  is the only non-zero trilinear coupling. Assuming that the soft masses for the stops are equal at the weak scale has some implications on the value of the light Higgs mass while as we just argued other assumptions about universality of sfermion masses should not impact much our analysis. On the other hand the gaugino mass relation should certainly be considered as a theoretical bias. This assumption is however well motivated in the context of models defined at the GUT scale. Most importantly in our approach we keep the higgsino parameter  $\mu$  and the gaugino mass  $M_2$  as completely

independent parameter. The relation between the gaugino and higgsino parameters is what determines the nature of the LSP and plays an important role in determining the LSP-LSP annihilation in the early universe. In that sense our model has many similarities with the non-universal Higgs model which also has  $\mu$  and  $M_2$  as independent parameters [28].

The observables selected to constrain the model include the relic density of dark matter,  $\Omega h^2$ , direct searches for Higgs and new particles at colliders, searches for rare processes such as the muon anomalous magnetic moment as well as various B-physics observables. Note that the dark matter relic abundance is computed within the standard cosmological scenario. The direct detection of dark matter while providing stringent constraint on the model introduces additional unknown parameters both from astrophysics and from strong interactions. We therefore prefer to consider the direct detection rate as an observable to be predicted rather than as a constraint keeping in mind that folding in the astrophysical and hadronic uncertainty could however easily introduce an order of magnitude uncertainty in that prediction [29, 30].

We find that each individual parameter of the MSSM model is only weakly constrained, in particular the parameters of the sfermion sector. The very large allowed parameter space as well as the prior dependence we observe only reflects the still poor sampling of the total parameter space by experiments. The neutralino sector is better constrained with a preferred value for the LSP of a few hundred GeV's and a small likelihood for masses above 900 GeV(600 GeV) with linear(log) priors, similarly charginos above 1.2 TeV(700 GeV) are disfavoured. We also find a lower limit on the pseudoscalar mass as well as on  $\tan \beta$ , this parameter also displaying a strong prior dependence. Furthermore some correlations between parameters of the model are observed, most notably the one between  $\mu$  and the gaugino mass. This is because those two parameters determine the higgsino content of the LSP.

After having determined the allowed parameter space, we examined the predictions for direct detection as well as for LHC searches both in the Higgs and SUSY sector as well as for B-physics observables. Although each type of search can only probe a fraction of the total parameter space we find a good complementarity between the different searches with less than 10% of scenarios leading to no signal. For example large signals for direct detection are expected in the mixed bino/Higgsino LSP scenario that are hard to probe at the LHC. The LHC searches in the SUSY and Higgs sector are also complementary and B-observables are specially useful in scenarios with large  $\tan \beta$  and a pseudoscalar that is not too heavy. The predictions for SUSY searches can be different from that expected in the constrained CMSSM with in particular a large fraction of models that only have a gluino accessible at LHC, the squarks being too heavy. To ascertain how experiments that will take place in the near future could further constrain the parameter space of the model we discuss the impact of a signal in  $B(B_s \to \mu^+ \mu^-)$  at Tevatron or of the observation of a signal in direct detection experiments. Finally we examine in more details the SUSY signals at the LHC, analysing the preferred decay chains for models that have either a gluino or a squark within the reach of the LHC. In this analysis we did not include the constraints from indirect detection experiments because the rates predicted feature a strong dependence on additional quantities such as the dark matter profile or the boost factor. The predictions for the rates for  $\bar{p}, e^+, \gamma$  will be presented in a separate publication [31].

The paper is organised as follows. The model and the impact of various constraints are described in section 2. The method used for the fit is described in section 3. The results of the global fits are presented in section 4 together with the impact of a selected number of future measurements. The SUSY signatures are detailed in section 5. The conclusion contains a summary of our results.

## 2 Model and constraints

We consider the MSSM with input parameters defined at the weak scale. We assume minimal flavour violation, equality of the soft masses between sfermion generations and unification of the gaugino mass at the GUT scale. The latter leads to  $M_2 \approx 2M_1 \approx M_3/3$ at the weak scale (relaxing this assumption is kept for a further study). We allow for only one non-zero trilinear coupling  $A_t$ . For the b-squark, the mixing which is  $\propto A_b - \mu \tan \beta$ is driven in general by  $\mu \tan \beta$  rather than by the trilinear coupling, this approximation is however not very good in the small sample of models with  $\mu \approx 100 \,\text{GeV}$ . Note also that the Higgs mass at high  $\tan\beta$  can show some dependence on the sbottom mixing. For first and second generations of squarks, the mixing which depends on fermions masses is negligible except for the neutralino-nucleon cross section since the dominant contributions to the scalar cross section are also dependent on fermion masses. However since the squark exchange diagram is usually subdominant as compared to Higgs exchange, the neglected contribution of the trilinear coupling falls within the theoretical uncertainties introduced by the hadronic matrix elements [30]. Similarly neglecting the the muon trilinear mixing,  $A_{\mu}$ , could affect the prediction for  $(g-2)_{\mu}$  but this effect is not large compared with the uncertainties on the value extracted from measurements. The top quark mass  $m_t$  is also used as an input although it has a much weaker influence on the results than in the case of GUT scale models. For the latter the top quark mass enters the renormalization group evolution and can have a large impact on the supersymmetric spectrum in some regions of the parameter space. In the general MSSM the top quark mass mainly influences the light Higgs mass. We fix  $\alpha_s(M_Z) = 0.1172$  and  $m_b = 4.23$  GeV. The free parameters of our MSSM model with unified gaugino masses, which we will refer to as MSSM-UG, are

$$\mu, M_2, M_{\tilde{l}}, M_{\tilde{q}}, A_t, \tan\beta, M_A, m_t \tag{2.1}$$

The range examined for each of these parameters is listed in table 1. MSSM-UG has a far more restricted set of parameters than the general MSSM, still this model will show how the possibilities for SUSY scenarios open up. The observables that will be used in the fit are listed in table 2. We first review the expectations for the role of each observable in constraining the MSSM parameter space.

The most powerful constraint is  $\Omega h^2$ . Since in the MSSM with gaugino universality there are four different mechanisms for efficient neutralino annihilation each calling for a different combination of SUSY parameters, each individual parameter is weakly constrained when exploring the full parameter space of the model. The main mechanisms for neutralino annihilation are:

stands for	General range
$\mu$ parameter	$[-3000, 3000] \mathrm{GeV}$
Gaugino mass, $2M_1 = M_2 = M_3/3$	$[30,2000]{\rm GeV}$
Common slepton mass, $M_{\tilde{l}} = m_{\tilde{\ell}_{L,R}}$	$[50,4000]\mathrm{GeV}$
Common squark mass, $M_{\tilde{q}} = m_{\tilde{q}_{L,R}}$	$[50,4000]{\rm GeV}$
Trilinear coupling of $\tilde{t}$	$[-3000, 3000] \mathrm{GeV}$
aneta	[5, 65]
Mass of CP-odd Higgs boson	$[100,2000]\mathrm{GeV}$
mass of $t$ -quark	$[165, 180]\mathrm{GeV}$
	stands for $\mu$ parameter Gaugino mass, $2M_1 = M_2 = M_3/3$ Common slepton mass, $M_{\tilde{l}} = m_{\tilde{\ell}_{L,R}}$ Common squark mass, $M_{\tilde{q}} = m_{\tilde{q}_{L,R}}$ Trilinear coupling of $\tilde{t}$ tan $\beta$ Mass of CP-odd Higgs boson mass of t-quark

Table 1. Range of the free parameters of MSSM-UG.

- annihilation of a bino LSP into fermion pairs, this necessitates light right-handed sfermions.
- annihilation of a mixed bino/higgsino into W pairs, this means  $\mu \approx M_1$ . Some contribution from chargino and neutralino coannihilations is also expected.
- annihilation near a (light or heavy) Higgs resonance, a LSP with a non-zero higgsino component is required but the higgsino fraction can be very small if  $m_{\tilde{\chi}_1^0} \approx m_h/2$ . For heavy Higgs exchange this process is more efficient at large  $\tan \beta$  due to the enhanced couplings of the heavy Higgs to b-quarks and  $\tau$  leptons.
- Coannihilation with sfermions, this usually means those of the third generation since they are lighter due to mixing. Recall that we are assuming only one slepton mass  $M_{\tilde{i}}$  and one squark mass  $M_{\tilde{q}}$ .

The lower limit on the Higgs mass from LEP strongly constrains the small tan  $\beta$  region. The upper range for the top quark mass and/or a large mixing in the stop sector are favoured. The latter means large values of  $|A_t|$ .

The muon anomalous magnetic moment still indicates a  $3\sigma$  deviation from the SM expectations [32]. The SUSY loop contributions can lead to  $\delta a_{\mu} > 0$  when sparticles are light. This is the case for the chargino/sneutrino loop and the neutralino/smuon loop when  $\mu > 0$ . The latter is enhanced at large values of  $\tan \beta$ , in this case it is easier to accomodate  $\delta a_{\mu} > 0$  even with a SUSY spectrum at TeV scale. Recall that we have neglected  $A_{\mu}$ , although the mixing is usually dominated by  $\mu \tan \beta$ , this introduces some restriction on the parameter space.

The branching ratio for  $B(b \to s\gamma)$  depends on the squark and gaugino/Higgsino sector as well as on the charged Higgs. A light pseudoscalar mass is permitted only if squarks are light as well. The squarks then partially cancel the large pseudoscalar contribution but only for  $\mu > 0$ . Furthermore when  $\mu > 0$ , the chargino contribution is negative relative to the SM one so  $B(b \to s\gamma)$  can drop too low for light charginos. This is particularly true when  $A_t$  is large and negative, meaning a large mixing in the stop sector. The process  $B(B_s \to \mu^+ \mu^-)$  receives SUSY loops contributions from Higgs exchange as well as from chargino and sfermions. In particular the amplitude for Higgs exchange is enhanced as  $\tan^3 \beta$ . The largest contribution are therefore expected for large  $\tan \beta$  and light  $M_A$ , particularly for light charginos and sleptons.

In the MSSM, the branching ratio for  $B_u \to \tau \nu_{\tau}$  is suppressed relative to the standard model prediction by the charged Higgs contribution. This contribution is enhanced as  $\tan^2 \beta$ . We will use the observable  $R(B_u \to \tau \nu_{\tau})$  which gives the ratio between the SUSY and SM predictions. Due to large uncertainties in hadronic matrix elements the standard model branching fraction is not known with a good precision, so this observable is not as powerful as other B-physics observables to constrain the parameter space of the MSSM.

LEP limits on the light Higgs and on sparticles constrain the chargino and neutralino sector as well as the charged sfermions. We have not included the recent Tevatron limits on the squark and gluino mass as well as the limits on the chargino mass from the trilepton search. When presenting our results we will comment on the impact of the new Tevatron results.<sup>1</sup>

## 3 Parameter sampling method

In this section we attempt to motivate the MCMC method in a heuristic way, for a detailed treatment see ref. [33]

The likelihood L is the probability distribution function (PDF) p(d|m) for a data set d being reproduced by an assumed model m. In our case, we assume the model m =MSSM-UG and the data set to be reproduced is given in table 2. This is a *top-down* approach where by varying the model parameters we find a suitable m to maximise p(d|m). However, in a *bottom-up* approach one would like to know the probability of model m being correct once given the data d, i.e. p(m|d). From Bayes' theorem we have

$$p(m|d) = p(d|m)\frac{p(m)}{p(d)},$$

where p(m) is the (absolute) probability of the model m being correct and p(d) is the total probability of reproducing the data d for all possible models. The p(d) is hard to estimate since it requires knowledge of all possible models. Thus, the absolute value of p(m|d) is hard to estimate. However, it is possible to estimate the *relative correctness* of a model  $m_1$  against another model  $m_2$  given the data d by taking the ratio

$$\frac{p(m_1|d)}{p(m_2|d)} = \frac{p(d|m_1) \ p(m_1)}{p(d|m_2) \ p(m_2)}$$

For simplicity, we take  $p(m_1) = p(m_2)$ , that is the probability of two models being correct is the same or we chose a flat prior over the model space. In this paper this translates to

<sup>&</sup>lt;sup>1</sup>Note that the trilepton search in  $pp \to \tilde{\chi}_1^+ \tilde{\chi}_2^0$  extends the LEP constraint on the chargino mass only when sfermions are light, no constraint is found in the large scalar mass limit (large  $m_0$ ) at least in the context of the CMSSM. The large fraction of our models which have heavy squarks will therefore not be probed by the Tevatron even if they feature light neutralinos and charginos.



Figure 1. Details of the MCMC algorithm used in this paper. Xa and Xb are the points in the parameter space, Oa and Ob are the values of the observables at points Xa and Xb respectively, La and Lb are corresponding likelihoods and fra and frb are the frequencies at two points.

using a flat prior over the parameter space of MSSM-UG as listed in table 1. Thus with flat prior we have

$$\frac{p(m_1|d)}{p(m_2|d)} = \frac{L(m_1)}{L(m_2)}.$$

This clearly hints that if we sample the parameter space using a directed random walk with transition probability proportional to  $\min(1, L(m_1)/L(m_2))$ , the sampling density will be proportional to the likelihood ratio or the relative correctness of the model. The details can be found in [33] and a representation of the algorithm used is given in figure 1.

There are two points in order: for the sampling density to be proportional to the ratio of the likelihoods the proposal PDF,  $Q(\mathbf{X}, \mathbf{X}_{a})$ , should be symmetric about  $\mathbf{X}_{a}$ , where  $\mathbf{X}, \mathbf{X}_{a}$ 

Observable	Limit	Likelihood function
$\delta a_{\mu}$	$(27.8 \pm 8.5) \times 10^{-10} \ [32]$	$\mathbf{G}(x, 27.8 \times 10^{-10}, 8.5 \times 10^{-10})$
$B(b \rightarrow s\gamma)$	$(3.55 \pm 0.24) \times 10^{-4}$ [34]	$\mathbf{G}(x, 3.55 \times 10^{-4}, 0.24 \times 10^{-4})$
$\Omega h^2$	$0.113 \pm 0.0105$ [7]	$\mathbf{G}(x, 0.113, 0.0105)$
$B(B_s \to \mu^+ \mu^-)$	$\leq 0.8 \times 10^{-7} \ [35]$	$\mathbf{F}(x, 0.8 \times 10^{-7}, -0.8 \times 10^{-9})$
$R(B \to \tau^+ \nu)$	$1.11 \pm 0.52$ [36, 38]	$\mathbf{G}(x, 1.11, 0.52)$
$m_h$	$\geq 114.5  \text{GeV}  [37]$	$\mathbf{F}(x, 114.5, 0.6)$
$m_t$	$171.4 \pm 2.1  \text{GeV}  [38]$	$\mathbf{G}(x, 171.4, 2.1)$

Table 2. Observables used in the global fit along with corresponding likelihood functions.

are points in the parameter space. We use the Gaussian distribution with the proposal PDF,

$$Q(\mathbf{X}, \mathbf{X}_{\mathbf{a}}) = \prod_{i} \exp\left[\frac{-(X^{i} - X_{a}^{i})^{2}}{2 (\Delta X^{i})^{2}}\right].$$
(3.1)

This will be called linear prior as the proposal function chooses the next point in the parameter set **X** within a linear scale, i.e. the points  $X_a^i \pm \Delta X_i$  have the same probability of being proposed. Replacing  $X^i, X_a^i$  with  $\log(X^i), \log(X_a^i)$  in the definition of  $Q(\mathbf{X}, \mathbf{X}_a)$  leads to log prior. That is, the points  $X_a^i(1 + \Delta X^i)$  and  $X_a^i/(1 + \Delta X^i)$  have the same probability of being proposed. We perform the global fits with both linear and log priors.

The second point is about the definition of likelihood. The likelihood L is a product of likelihood for each of the observables. For the observable with definite measurement, the likelihood function is a Gaussian

$$\mathbf{G}(O, O_{\mathrm{exp}}, \Delta O) = \exp\left[\frac{-(O - O_{\mathrm{exp}})^2}{2 \ (\Delta O)^2}\right]$$

Here,  $O_{exp}$  is the central value of the observable,  $\Delta O$  is the  $1\sigma$  error and O is the value of the observable at the proposed point **X** in parameter space. For observables with upper/lower limits the likelihood function is a smooth step-like function

$$\mathbf{F}(O, O_{\exp}, \Delta O) = \frac{1}{1 + \exp[\pm (O - O_{\exp})/\Delta O]}$$

The positive sign is for the lower limit and the negative sign for the upper limit. Here  $O_{\text{exp}}$  is the 95% exclusion limit and  $\Delta O$  is about 1% of  $O_{\text{exp}}$  to roughly emulate the 95% exclusion limit. The list of observables used to calculate the likelihood is given in table 2 alongwith the corresponding experimental values or limits.

#### 4 Results

We have first scanned linearly over the 8 parameters of the MSSM-UG using the Markov Chain Monte Carlo (MCMC) method just described. To estimate the prior dependence we have also used the log priors. We run 10 chains each with  $10^6$  (6.10<sup>5</sup>) likelihood evaluations for linear (log) prior. The chains show good convergence [39] for linear prior ( $\hat{R} - 1 = 0.15$ )

	Linear prior				Log prior			
Parameter 68% interval		95% interval		68% interval		95% interval		
$\mu \; [\text{GeV}]$	197.7	1193	-983.5	2471	-158.9	560.1	-850.9	2001
$M_2 \; [\text{GeV}]$	259.8	1077	119.6	1845	102.2	524.0	102.2	1252
$M_{\tilde{l}} \; [\text{GeV}]$	398.4	2270	225.4	3700	100.0	1591	100.0	3582
$M_{\tilde{q}} \; [\text{GeV}]$	1824	3602	1236	3938	1514	4006	1001	4006
$A_t \; [\text{GeV}]$	-1735	2239	-2785	2876	-337.6	814.0	-2113	2430
an eta	19.5	65.0	8.15	65.0	4.85	39.7	4.85	58.9
$M_A \; [\text{GeV}]$	537.1	1489	370.2	1904	475.0	1130	338.0	1759
$m_t \; [\text{GeV}]$	169.6	173.7	167.6	175.6	169.7	173.8	167.7	175.8

Table 3. The BC intervals of the MSSM-UG parameters.

while for log priors the convergence is a bit poor  $(\hat{R} - 1 = 3.15)$  since parameters like  $\mu$ and  $A_t$  can not change their sign in the same chain with log priors. However, if we choose a subset of chains with the same sign of  $\mu$  and  $A_t$ , the convergence can be as good as  $\hat{R} - 1 = 10^{-3}$ . In both cases, the particle spectrum was computed by SoftSusy2.0 [40] and fed to micrOMEGAs2.2 [30, 41, 42] for the computation of all DM observables as well as of constraints on the parameters of the supersymmetric model. The SM value for the branching  $B(b \to s\gamma)$  calculated in [41] was shifted in order to match the NNLO result of [43].

The range chosen for all parameters is listed in table 1 and the six observables used in the fit listed in table 2.<sup>2</sup> In addition we have imposed the LEP limits on sparticles  $(m_{\tilde{\chi}_1^+}, m_{\tilde{l}}...)$  as defined in micrOMEGAs2.2 and for the likelihood we have assumed a binary step function. We then examined the allowed regions for each input parameter as well as the predictions for physical parameters and observables. We have not imposed the Tevatron limit on gluino and squarks  $m_{\tilde{g}} > 308 \text{ GeV}$  and  $m_{\tilde{q}} > 379 \text{ GeV}$  [45]. However after fitting the model we have checked a posteriori that these constraints did not affect much our analysis. Because of the universality condition, the gluino mass limit is always satisfied while the squark limit is not satisfied in less than one per-mil of our scenarios.

## 4.1 The allowed parameter space of the MSSM

We found wide allowed regions for each model parameter, the distributions are displayed in figure 2 and the 68% and 95% Bayesian credibility(BC) intervals in table 3. As expected the log priors put more weight on the lower end of the range used in the scan.

- As expected,  $\mu > 0$  is preferred, this is mainly due to the  $B(b \to s\gamma)$  and  $\delta a_{\mu}$  constraints. Note however that one can get a reliable global fit even with  $\delta a_{\mu} = 0$  so that the 95% BC interval extends to the negative  $\mu$  region, see table 1.
- The gaugino mass reaches almost the maximum value probed,  $M_2 < 1845 \,\text{GeV}$  with 97.5% BC. Charginos above the TeV scale are somewhat disfavoured (see the 68%

<sup>&</sup>lt;sup>2</sup>The upper limit on  $B(B_s \to \mu^+ \mu^-)$  has improved to  $0.58 \times 10^{-7}$  [44]. We have checked a posteriori that this improvement did not affect much our analysis.



Figure 2. The posterior PDF of the model parameters is shown for linear priors (thin black line) and log priors (thick gray/green line).

BC interval at 1.1 TeV with linear priors and 524 GeV with log priors) because they give little contribution to  $\delta a_{\mu}$ , furthermore the light neutralinos LSP annihilate more efficiently except when they have a large Higgsino component or can annihilate near a resonance.

- For linear priors, the slepton mass distribution is peaked at 500 GeV with a long tail that extends to almost the upper limit of the region scanned. The sleptons just above the LEP limit are disfavoured with 95% BC interval being  $M_{\tilde{l}} \in [225, 3700]$  GeV for linear prior. This shows that although light sleptons can contribute to the annihilation of a bino LSP and to  $\delta a_{\mu}$ , present data can be accommodated with heavy sleptons. With the log priors the light sleptons are preferred and can even lie just above the LEP exclusion limit. Nevertheless the distribution features a long tail that extends near the upper limit of the region scanned.
- Heavy squarks are preferred, we have  $M_{\tilde{q}} > 1.24$  (1.0) TeV with 97.5% BC for the linear (log) prior. Quarks below the TeV scale tend to give too large corrections to B-physics observables and in particular to  $B(b \rightarrow s\gamma)$ . Although the quark contribution can be compensated by that of a light pseudoscalar, this requires fine-tuning and has a small likelihood. There is no upper limit on the squark mass as it can reach the upper limit of the range used in the scan, 4 TeV.

- Light pseudoscalars are disfavoured, we have  $M_A > 370~(338)$  GeV with 97.5% BC for linear (log) prior. While it is possible to have a good fit to the data with lighter pseudoscalar masses this occur only after fine tuning the sfermion masses in order to satisfy both  $\delta a_{\mu}$  and  $B(b \rightarrow s\gamma)$ . Therefore these models have a small likelihood.
- The distribution for  $\tan \beta$  is skewed towards the upper range and  $\tan \beta > 8.15$  with 97.5% BC for linear prior. Large values of  $\tan \beta$  make it easier to escape the LEP bound on the Higgs mass, facilitate annihilation of the LSP through Higgs exchange and can also help explain  $\delta a_{\mu}$ . The distribution for  $\tan \beta$  is strongly shifted towards lower values and peaks around  $\tan \beta = 5$  for log priors owing to the inherent preference of log priors towards lower values of parameters.
- There are no preferred value for  $A_t$  although the distribution is skewed towards  $A_t > 0$ , see table 3.

A few correlations among input parameters are observed, see figure 3. These are driven to a large extent by the relic density constraint. First  $\mu$  and  $M_{\tilde{l}}$  are correlated: a large  $\mu$  requires light sleptons while heavy sleptons need  $\mu$  not much above the TeV scale. When sleptons are heavy the LSP must have a higgsino component to annihilate efficiently. Conversely when  $\mu$  is large and the LSP is bino, light sleptons are needed for efficient annihilation into fermion pairs. Second  $M_2$  is also correlated with  $\mu$  and  $M_A$ : when  $M_2$  exceeds 1.2TeV, one needs either  $|\mu| \approx M_2/2 \approx M_1$  or  $M_2 \simeq M_A$ . The first correlation is strong and means that a heavy LSP with a significant higgsino component annihilates efficiently. The second correlation corresponds to  $m_{\tilde{\chi}_1^0} \approx M_A/2$  with the LSP annihilating near a heavy Higgs resonance. This correlation is weak as we have just mentionned, other large values of  $M_2$  are allowed when the LSP has a large higgsino component.

#### 4.2 The particle spectrum

From this allowed parameter space we can determine the favoured region for the masses of new particles that can be searched for at LHC.

- The light Higgs is SM like (i.e.,  $\eta^2 \approx 1$ ) and the mass prediction is  $m_h = 120.2^{+4.6}_{-4.9}$  GeV with 95% BC using linear prior and  $m_h = 118.4^{+5.2}_{-4.4}$  GeV with 95% BC using log prior.
- The 95% BC interval for the LSP mass is  $m_{\tilde{\chi}_1^0} \in [52.2, 873]$  GeV with linear priors and  $m_{\tilde{\chi}_1^0} \in [52.9, 584]$  GeV with log priors. The lower bound results from the assumption of GUT scale gaugino mass universality and the LEP limit on charginos. The peak in the distribution around 55–60 GeV corresponds to LSP annihilation near a light Higgs resonance.
- The lightest chargino (as well as  $\tilde{\chi}_2^0$ ) could be just above the LEP reach and lies below  $m_{\tilde{\chi}_1^+} < 1180$  (770) GeV with 97.5% BC for linear (log) priors. There is a peak in the distribution near 100GeV which is correlated with the LSP peak corresponding to annihilation near the light Higgs.



**Figure 3.** 2D contours for  $M_{\tilde{l}} - \mu$  (left panel)  $M_2 - \mu$  (middle panel)  $M_A - M_2$  (right panel) showing the 68% BC (dark grey) and 95% BC (light grey) contours. The top panels are with linear priors and the bottom panels with log priors.

- The gluino mass is related to the neutralino mass via the universality condition, the 97.5% BC lower limit gives  $m_{\tilde{g}} > 478 \,\text{GeV}$  and the maximum can exceed 5 TeV using linear priors. However we have  $m_{\tilde{g}} < 3.3 \,\text{TeV}$  with 84% BC, which is slightly beyond the reach of the LHC with maximum luminosity. With log priors the gluino is restricted to  $m_{\tilde{g}} < 3.7 \,\text{TeV}$  at 97.5% BC.
- As mentionned before, squark masses are in the TeV range. Because of the universality assumption on squark masses the mixing in the stop sector implies that the stop is the lightest squark. We find  $m_{\tilde{t}_1} > 1130(910)$  GeV with 97.5% BC for linear (log) priors. Squark masses can reach all the way to the upper end of the range of the scan, 4TeV. There is no guarantee that squarks are within the reach of the LHC.
- Slepton masses reach almost all the way to 4TeV. Since masses of sleptons and gauginos are uncorrelated, a large fraction of scenarios have  $m_{\tilde{l}_{1,2}} > m_{\chi_2^0}, m_{\tilde{\chi}_1^+}$  (around 75% of allowed scenarios for linear priors). For these scenarios the preferred decay channel of  $\tilde{\chi}_2^0$  is three body and has a branching fraction around 3% into each flavour of charged lepton. In this model all slepton masses are identical except for mixing effect so only one mass is displayed in figure 4.

The higgsino fraction of the LSP strongly influences the properties of the DM,  $f_H = |N_{13}|^2 + |N_{14}|^2$  where the neutralino mixing matrix is defined in the basis  $\tilde{\chi}_1^0 = N_{11}\tilde{B} +$ 

68% interval		95% interval	
115.7	121.0	114.0	123.6
475	1130	338	1759
69.1	249	52.9	584
126	404	107	770
130	728	130	2061
269	911	231	2066
112	399	103	768
266	905	226	2050
114	1598	114	3590
114	1594	114	3586
96.4	1586	96.4	3584
123	1600	123	3590
1535	3422	1019	3934
1541	3436	1024	3950
1545	3442	1027	3956
1542	3436	1025	3949
1524	3413	1003	3924
1542	3430	1028	3940
1500	3389	911	3897
1560	3424	1086	3934
637	1757	442	3764
$5.49 \ 10^{-3}$	0.359	$4.91 \ 10^{-4}$	0.604

Log prior

Table 4. The 68% and 95% BC interval for sparticle masses and for the higgsino fraction.

Linear prior

122.6

0.297

95% interval

115.3

52.2

 $3.39 \ 10^{-4}$ 

124.8

0.659

68% interval

117.6

52.2

 $1.58 \ 10^{-3}$ 

Mass

 $m_h$ 

 $m_H$ 

 $\begin{array}{c} m_{\tilde{\chi}^0_1} \\ m_{\tilde{\chi}^0_2} \end{array}$ 

 $\begin{array}{c} m_{\tilde{\chi}^0_3} \\ m_{\tilde{\chi}^0_4} \end{array}$ 

 $m_{\tilde{\chi}_1^+}$ 

 $m_{\tilde{\chi}_2^+}$ 

 $m_{\tilde{e}_L} \\ m_{\tilde{e}_R}$ 

 $m_{\tilde{\tau}_1}$ 

 $m_{\tilde{\tau}_2} \\ m_{\tilde{u}_L}$ 

 $\begin{array}{c} m_{\tilde{u}_R} \\ m_{\tilde{d}_L} \end{array}$ 

 $m_{\tilde{d}_R}$ 

 $m_{\tilde{b}_1} \\ m_{\tilde{b}_2}$ 

 $m_{\tilde{t}_1}$ 

 $m_{\tilde{t}_2}$  $m_{\tilde{g}}$ 

 $f_H$ 

 $N_{12}\tilde{W} + N_{13}\tilde{H}_1 + N_{14}\tilde{H}_2$ . The higgsino fraction spans a wide range  $3.4 \times 10^{-4} < f_H < 0.66$ with 95% BC interval for linear prior. The distribution is peaked around  $0.15 < f_H < 0.35$ for both priors. A small higgsino fraction is found either for light LSP's and for LSP's annihilating near a Higgs resonance. The higgsino fraction has an impact on the spectrum and in particular on the mass difference  $m_{\tilde{\chi}_1^+} - m_{\tilde{\chi}_1^0}$ . A large mass difference is expected for a small higgsino fraction (since in that case  $m_{\tilde{\chi}_1^+}/m_{\tilde{\chi}_1^0} \approx 2$ ) whereas when  $f_H > 0.15$ ,  $m_{\tilde{\chi}_1^+} - m_{\tilde{\chi}_1^0} < M_W$  and  $m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0} < M_Z$ . This means that for a large number of scenarios that satisfy this condition the decay channels  $\tilde{\chi}_1^+ \to \tilde{\chi}_1^0 W$ ,  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 Z$  are forbidden and only 3-body decays are possible since sleptons are often heavier than the chargino.

# 4.3 Other observables

Form the allowed parameter space we then examine the predictions for the observables used in the fit together with the direct detection cross-section.

• The observables  $\Omega h^2$  and  $B(b \to s\gamma)$  are well distributed around the central values



JHEP11(2009)026

**Figure 4.** The posterior PDFs for sparticle masses:  $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_1^+}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_2^+}, m_{\tilde{g}}, m_h, m_{\tilde{e}_L}, m_{\tilde{t}_1}$  and for the higgsino fraction,  $f_H$ . The scale on the y-axis is adjusted to have same maximum value for both linear priors (thin black line) and log priors (thick gray/green line).

used in the fit. As expected,  $B(b \to s\gamma)$  lies near the upper end of the allowed range for small  $M_A, \mu, M_2$  and  $M_{\tilde{l}}$  and are enhanced at very large values of  $\tan \beta$ .

- The branching ratio  $B(B_s \to \mu^+ \mu^-)$  is peaked around  $2.5 \times 10^{-9}$  and for the linear priors a long tail extends to  $2. \times 10^{-8}$  with 95% BC. Values near the upper limit are found for  $M_A < 600 \text{ GeV}$ ,  $\tan \beta > 50$ , for not too heavy charginos,  $m_{\tilde{\chi}_1^+} < 750 \text{ GeV}$ and for a LSP with a small higgsino fraction,  $f_H < 0.05$ . With log priors the distribution drops sharply after the peak value, large branching ratios are very unlikely.
- We have R(B → τν) > 0.38 (0.48) with 97.5% BC for linear (log) priors, as for other B-physics observables, the largest suppression to R(B → τν) are found for small M<sub>A</sub>, μ, M<sub>2</sub> and M<sub>l</sub> as well as for tan β > 50.
- The muon anomalous magnetic moment extends over more than an order of magni-

	Linear prior				
Observable	68% in	terval	95% interval		
$\Omega h^2$	0.102	0.123	0.091	0.133	
$\delta a_{\mu} \times 10^{10}$	1.49	27.2	-1.45	37.5	
$B(B \to X\gamma) \times 10^4$	3.19	3.62	3.08	3.86	
$B(B_s \to \mu^+ \mu^-) \times 10^9$	1.82	3.31	1.48	20.4	
$R(B \to \tau \nu)$	0.698	0.981	0.382	0.997	
$\sigma_{\chi p}^{SI}$ (pb)	$2.51 \ 10^{-10}$	$6.76 \ 10^{-8}$	$9.77 \ 10^{-12}$	$2.24 \ 10^{-7}$	
	Log prior				
Observable	68% in	terval	95% interval		
$\Omega h^2$	0.102	0.123	0.092	0.134	
$\delta a_{\mu}  imes 10^{10}$	-0.58	33.5	-3.23	42.4	
$B(B \to X\gamma) \times 10^4$	3.25	3.73	3.12	3.97	
$B(B_s \to \mu^+ \mu^-) \times 10^9$	2.29	3.02	1.60	3.68	
1	1		0 170	1 000	
$R(B \to \tau \nu)$	0.808	1.000	0.476	1.000	

Table 5. The BC intervals for the observables.

tude and in particular can include negative values. The peak of the distribution with linear priors lies near  $10^{-10}$ , much below the central experimental value we have used indicating that our model does not provide a good fit to this observable. Large values of  $\delta a_{\mu}$  are found for light sleptons and neutralinos/charginos, this is why a better fit to the data is found for low values of  $M_2$  and  $M_{\tilde{l}}$ .<sup>3</sup> This is illustrated in figure 7a,b. This observable also plays a role in setting the upper limit on the neutralino/chargino masses. For log priors two solutions are found, one strongly peaked at a small negative value for  $\delta a_{\mu}$  and the second with a broad distribution around the central value used in the fit. Because the MC chains cannot migrate from a positive  $\mu$  to a negative  $\mu$  solution, the weight of each solution depends on the random choices made for the starting points of the different chains (2 chains with -ve  $\mu$  and 8 chains with +ve  $\mu$ ).

The dependence of the B-observables on some of the most relevant parameters are displayed in figure 7 (c)–(i) for linear priors and in figure 8 (c)–(i) for log prior, in particular the enhancement for  $B(B_s \to \mu^+\mu^-)$ ,  $B(b \to s\gamma)$  and  $R(B \to \tau\nu)$  with the light pseudoscalar mass. In fact a heavy pseudoscalar leaves little prospects for observing large deviations in B-observables,  $M_A > 1$  TeV implies  $B(B_s \to \mu^+\mu^-) < 5 \times 10^{-9}$  and  $R(B \to \tau\nu) > 0.70$ . Similarly small values of tan  $\beta$ , for example tan  $\beta < 20$ , implies  $B(B_s \to \mu^+\mu^-) < 2.5 \times 10^{-9}$ and  $R(B \to \tau\nu) > 0.85$ . The potential enhancement at large values of tan  $\beta$  is illustrated only for  $B(B_s \to \mu^+\mu^-)$ . The largest values for  $B(B_s \to \mu^+\mu^-)$  are also found at low values of  $M_2$ , they are therefore correlated with large deviations in  $\delta a_{\mu}$  [47]. The deviation

<sup>&</sup>lt;sup>3</sup>If  $\delta a_{\mu}$  turns out to be consistent with the SM prediction, as indicated by some preliminary results [46], the distributions for  $M_2, M_{\tilde{l}}$  would shift to larger values.



JHEP11(2009)026

**Figure 5.** The posterior PDFs for  $B(b \to s\gamma)$ ,  $B(B_s \to \mu^+\mu^-)$ ,  $\delta a_{\mu}$  and  $\sigma_{\chi p}^{SI}$ . The scale on the y-axis is adjusted to have same maximum value for both linear priors (thin black line) and log priors (thick gray/green line).

from SM expectations for B-observables are more modest in the case of log priors, this is because small values of  $\tan \beta$  are favoured.

The predictions for the neutralino nucleon elastic scattering,  $\sigma_{\chi p}^{SI}$ , vary over 5 orders of magnitude for both sets of priors. The distributions peak at values near the experimental upper limit, see figure 5 and can even exceed the present limit. The LSP mass dependent CDMS limit is displayed in figure 6a [2]. The light Higgs exchange in general dominate SI interactions. Therefore large cross sections are expected when the LSP has a large coupling to the light Higgs, this means some higgsino component, figure 6d. For example a LSP with a higgsino component  $f_H > 0.2$  necessarily implies  $\sigma_{\chi p}^{SI} > 3.2 \times 10^{-9}$  pb for linear priors. These values will be probed in the near future with for example Xenon100 [12]. On the other hand a pure bino LSP has a cross section at least two orders of magnitude below the experimental limit. The second Higgs scalar as well as squarks can also contribute



**Figure 6.** Predictions for elastic scattering cross sections as a function of  $m_{\tilde{\chi}_1^0}$ ,  $\mu$ ,  $M_A$  and  $f_H$ . Default values of micrOMEGAs2.2 for the quark content of the nucleon are taken. On the left panel the CDMS-II exclusion is shown by a solid line, while the dashed line shows the factor 10 improved limits. The top panel is with linear priors and the bottom panel with log priors.

significantly when they have a mass comparable to the LSP. There is however no direct correlation between the direct detection rate and  $M_A$ , figure 6c. Note that the enhancement of the heavy Higgs contribution relative to the light Higgs expected at large values of tan  $\beta$  is tamed because the pseudoscalar is always much heavier than the light Higgs.

#### 4.4 Complementarity of different LHC searches and direct dark matter searches

From the above discussion, it is clear that B-physics observables,  $\delta a_{\mu}$ , direct detection as well as direct particle searches at LHC are sensitive to different sectors of the MSSM. Direct searches at LHC are especially powerful to probe the coloured sector while heavy Higgs searches probe the large tan  $\beta$ . Direct detection probes best the higgsino LSP.

To illustrate quantitatively the complementarity of the various new physics signals at LHC and in direct detection we compute the fraction of models in the allowed parameter space that lead to a signal in 4 different channels: direct searches of sparticles at LHC, searches for heavy Higgs at LHC, deviation in  $B(B_s \to \mu^+ \mu^-)$  and DM direct detection. Here we choose  $B(B_s \to \mu^+ \mu^-)$  as a representative observable from the B-sector to simplify the discussion. The same exercise with another B-observable would lead to a similar conclusion. The signal in each channel is defined as follows. We assume that coloured sparticles are within reach at LHC-14TeV if their mass is below 2 TeV. This corresponds roughly to the reach for gluinos when squarks are heavy and  $\mathcal{L} = 60 f b^{-1}$  [16, 17]. This value for the squarks reach is conservative but we use it for simplicity, recall that with a



Figure 7. 2D contours for some observables with linear prior, from top left to bottom right: (a)  $\delta a_{\mu} - M_{\tilde{l}}$  (b)  $\delta a_{\mu} - m_{\tilde{\chi}_{1}^{0}}$  (c)  $B(B_{s} \to \mu^{+}\mu^{-}) - M_{\tilde{l}}$  (d)  $B(B_{s} \to \mu^{+}\mu^{-}) - A_{t}$  (e)  $B(B_{s} \to \mu^{+}\mu^{-}) - \tan \beta$  (f)  $B(B_{s} \to \mu^{+}\mu^{-}) - M_{A}$  (g)  $B(B_{s} \to \mu^{+}\mu^{-}) - M_{2}$  (h) $B(b \to s\gamma) - M_{A}$  (i)  $R(B \to \tau\nu) - M_{A}$ . The 68% BC contour is in dark grey and 95% BC contour in light grey.

high luminosity,  $\mathcal{L} = 300 f b^{-1}$ , coloured sparticles can be discovered up to 3 TeV. To define the discovery reach for the heavy Higgs we use the results of the CMS study which gives the discovery region in the  $\tan \beta - M_A$  plane for  $\mathcal{L} = 30 f b^{-1}$  [17]. This is based on the associated production of a Higgs with b-quarks,  $gg, qq \rightarrow b\bar{b}h$  with the Higgs decaying into tau pairs. In the MSSM, this process is accessible only at large values of  $\tan \beta$  because of the  $\tan \beta$ -enhanced couplings of the heavy Higgs to  $b\bar{b}, \tau\bar{\tau}$  pairs. For example the pseudoscalar mass can be probed up to  $M_A < 800$  GeV for  $\tan \beta = 50$ .

For the process  $B_s \to \mu^+ \mu^-$  we assume the value for the branching  $B(B_s \to \mu^+ \mu^-) <$ 



Figure 8. Same as figure 7 but with log prior. The 68% BC contour is in dark grey and the 95% BC contour in light grey.

 $5 \times 10^{-9}$  which will be probed even with a low luminosity at the LHC. Finally for the elastic scattering cross section our definition of a signal corresponds to one order of magnitude improvement over the current CDMS limit [2]. With various experiments increasing their sensitivities regularly, this level should be reached in the near future [12].

First we consider the case where sparticles are too heavy to be accessible at LHC. In these scenarios it is clearly essential to consider alternative signals of new physics and/or dark matter. In fact a large number of the allowed scenarios (almost 34% with linear priors and about 9% with log priors) predict a heavy coloured spectrum. We will refer to this as set A in the next section. This is easily explained by the fact that no observable

Linear prior						
Heavy Higgs at LHC	$\sigma_{\chi p}^{SI}(\text{ pb})$	$B(B_s \to \mu^+ \mu^-)$				
		$> 5. \times 10^{-9}$	$< 5. \times 10^{-9}$			
Yes	$20.6\% (> 10^{-9})$	5.6%	15%			
24.2%	$3.6\% (< 10^{-9})$	1.7%	1.9%			
No	$54.9\% (> 10^{-9})$	0.3%	54.6%			
75.8%	$20.9\% (< 10^{-9})$	0.7%	20.2%			
	Log prior					
Yes	$10.6\% (> 10^{-9})$	0.8%	9.8%			
11.4%	$0.8\% (< 10^{-9})$	0.1%	0.7%			
No	$63.0\% (> 10^{-9})$	< 0.1%	63.0%			
88.6%	$25.6\% (< 10^{-9})$	< 0.1%	25.6%			

**Table 6.** Prospects for Higgs searches, direct detection and  $B(B_s \to \mu^+ \mu^-)$  in scenarios with heavy coloured sparticles,  $m_{\tilde{q}}, m_{\tilde{g}} > 2 \text{ TeV}$ .

(except weakly for  $\delta a_{\mu}$ ) requires a supersymmetric contribution as long as the DM can give the proper relic abundance. The best alternative at LHC for a sign of physics beyond the standard model would be the search for a heavy  $Higgs^4$  with nearly 24.2% of scenarios predicting a signal while few deviations from the SM in  $B(B_s \to \mu^+ \mu^-)$  are expected (8.3%) of the scenarios in set A with linear priors and < 1% for log priors). Furthermore signals in B-physics are mostly found in scenarios for a light pseudoscalar Higgs and very large values of  $\tan \beta$  where one also has a heavy Higgs signal. The complementarity between the direct detection and collider searches is clearly evident in table 6. For linear priors, nearly half (54.9%) the models lead to a signal only in direct detection experiments and about 20.6% of models predict a signal in both the Higgs and the direct detection. For log priors nearly 75% of scenarios predict a signal in direct detection most of these predicting no heavy Higgs signal. Of course, these statements should be modulated by the fact that there are large theoretical and astrophysical uncertainties in the prediction of the neutralino proton scattering cross section. Combining all the channels we are left with a small fraction of models with no signal in SUSY or Higgs searches at colliders, B-physics or direct detection, the fraction corresponds to 20.2% (25.6%) of the subset with heavy sparticles which means about 7% (2%) of the sample of allowed scenarios with linear (log) priors. We have also checked that there are no other SUSY signals at LHC in these scenarios with heavy squarks and gluinos. We have computed the trilepton signal for direct neutralino/chargino production,  $pp \to \tilde{\chi}_i^0 \tilde{\chi}_1^+ \to 3l + E_T^{\text{miss}}$  and found a maximum cross section of a few fb at  $\sqrt{s} = 14$  TeV. The reasons for the small cross section are the heavy squarks and the heavy neutralinos and charginos, for linear priors the 97.5% BC lower limits are  $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0} > 285, 366, 371 \,\text{GeV}$  and  $m_{\tilde{\chi}_1^+} > 354 \,\text{GeV}$ , while for log priors the corresponding limits are  $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0} > 275, 360, 363 \text{ GeV}$  and  $m_{\tilde{\chi}_1^+} > 404 \text{ GeV}$ . The

 $<sup>^{4}\</sup>mathrm{Here}$  we have not included the possibility of discovering SUSY particles in Higgs decays

Linear prior					
Heavy Higgs at LHC	$\sigma_{\chi p}^{SI}$ (pb)	$B(B_s \to \mu^+ \mu^-)$			
		$> 5. \times 10^{-9}$	$< 5. \times 10^{-9}$		
Yes	$21.9\% (> 10^{-9})$	7.2%	14.7%		
24.5%	$2.7\% (< 10^{-9})$	1.6%	1.1%		
No	$53.7\% (> 10^{-9})$	0.6%	53.1%		
75.5%	$21.8\% (< 10^{-9})$	1.1%	20.7%		
	Log prior				
Yes	$12.8\% (> 10^{-9})$	1.1%	11.7%		
13.2%	$0.3\% (< 10^{-9})$	< 0.1%	0.3%		
No	$68.3\% (> 10^{-9})$	0.4%	67.9%		
86.8%	$18.5\% (< 10^{-9})$	0.1%	18.4%		

**Table 7.** Prospects for Higgs searches, direct detection and  $B(B_s \to \mu^+ \mu^-)$  in scenarios with light coloured sparticles,  $m_{\tilde{q}} < 2 \text{ TeV}$  or  $m_{\tilde{g}} < 2 \text{ TeV}$ .

direct production of sleptons is also below the LHC reach for  $30 f b^{-1}$  since the lower limit on slepton masses are  $m_{\tilde{e}_L}, m_{\tilde{e}_R} > 300 \text{ GeV}$  for both linear and log priors.

The results for the case where sparticles are accessible at LHC leads to roughly the same conclusion, see table 7. One difference is a small increase in the fraction of models that predict an observable deviation in  $B(B_s \to \mu^+ \mu^-)$ . This is particularly true if squarks below the 2TeV scale are present. In the case where both a heavy Higgs and squarks are accessible at LHC, more than a third of the models also predict  $B(B_s \to \mu^+ \mu^-) > 5. \times 10^{-9}$  with linear priors.

## 4.5 Impact of improved sensitivity

Rather than just looking at the discovery potential we also examine the impact of a signal in the near future in direct detection or in  $B(B_s \to \mu^+\mu^-)$ . First let us comment on the impact of the present CDMS limit on direct detection [2]. Recall that because of the astrophysical and nuclear uncertainties we have not used this observable in the fit. We applied this constraint a posteriori on the selected models and looked at the impact on the SUSY spectrum. The most noticeable effect of this constraint is that it removes some models with  $65 < m_{\tilde{\chi}_1^0} < 170 \text{ GeV}$  especially when those models have a large value for the higgsino fraction  $f_H$ . Models with  $m_{\tilde{\chi}_1^0} \approx 50 \text{ GeV}$  that have a small higgsino fraction are not affected. Furthermore some of the models with low values of  $M_A$  and large  $\tan \beta$ are disfavoured. To have an indication of the impact of a signal in direct detection we then considered the case of a signal  $\sigma_{\chi p}^{SI} = 1. \times 10^{-8}$  pb and allowed a factor 3 theoretical uncertainty. With such a measurement one could constrain the allowed parameter space although no specific correlation with other observables are observed, only a lower bound on the LSP higgsino fraction is found.

We have also considered the impact of a signal at the Tevatron in  $B(B_s \to \mu^+ \mu^-)$ , say  $B(B_s \to \mu^+ \mu^-) > 1.8 \times 10^{-8}$  which represents the ultimate reach of Tevatron [48]. We

found that in this case and with linear priors a lower bound on  $\tan \beta > 32$  with 97.5% BC could be extracted (though a tail extends till  $\tan \beta \sim 18$ ) and furthermore that a heavy Higgs signal at LHC would almost be guaranteed (in 94.6% of the scenarios). Finally the models with a signal within the Tevatron reach in  $B(B_s \rightarrow \mu^+\mu^-)$  all predict a small cross section in the trilepton channel ( $\sigma_{lll}^{\text{TeV}} < 0.1 \text{ fb}$ ) even before applying cuts. This points towards a complementarity between the two channels as was found in the MSSM [49]. However, as we have mentionned before only a small fraction of the MSSM-UG models are within the Tevatron reach for the trileptons.

## 5 LHC forecasts

At last we examine in more details the SUSY signatures at the LHC. To simplify the discussion we examine in details only the case of linear priors. For this we split the scenarios allowed at 95% BC in different sets according to which sparticles are within the reach of the LHC. We have already mentionned that a significant fraction (34%) of our scenarios predict a coloured spectrum that is just too heavy (set A). Another large fraction (42.1%) corresponds to the case where the gluino is the only coloured sparticle that could be discovered at LHC (set B) while a squark is also within reach in 15.5% (set C). In 8.4% of our scenarios (set D) only squarks are accessible. The main difference from the CMSSM is that in the latter the squark masses receive an important contribution from  $M_3$  due to the renormalization group running so the cases where only a gluino is accessible at LHC are confined to the focus point region. The precise fraction of models that have sparticles within reach of the LHC do depend on the range on the parameters used in the scan. In particular it is clear that a wider range for the squark masses would have led to a larger fraction of models with squarks too heavy to be produced at the LHC.

For each set of scenarios we then examine the main branching fractions of sparticles concentrating on squarks, gluinos and on the neutralino/charginos produced in their decay. Our goal is to point out the different decay channels available. We do not attempt to analyse the feasibility of extracting signals over background in our scenarios, this is beyond the scope of this paper.

Note that in some scenarios, the chargino/neutralino can be produced directly leading to a signal in the trilepton channel,  $p\bar{p} \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_1^+ \rightarrow 3l + E_T^{\text{miss}}$ . We do not here analyse direct production specifically but we have checked that the Tevatron only weakly constrains our allowed scenario, about 1 per-mil of our models have a trilepton cross section  $\sigma(3l + E_T^{\text{miss}}) >$ 0.08 pb before applying cuts.

## 5.1 Scenarios where $m_{\tilde{g}} < 2$ TeV, $M_{\tilde{q}} > 2$ TeV

In the MSSM-UG the scenarios where only gluinos are accessible at LHC represent a large fraction of the scenarios that provide a good fit to the data. To examine the characteristic decay chains in these scenarios, we have, for each point in our MCMC chain, computed the branching ratios of gluinos into neutralino/charginos as well as the 2- and 3-body branching ratios of  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_3^0$  with micrOMEGAs2.3. The decay chains involving a chargino can be dominant but we concentrate on the heavy neutralinos because the leptonic decay



Figure 9. Distribution of the gluino branching fractions in third generation quarks a) $B_{gQQ}$  b)  $Br(\tilde{g} \to \tilde{\chi}_i^0 Q Q)$ . There is a scale factor of 10<sup>6</sup> on the y-axis.

mode provide a clear signature and the kinematic endpoint in the lepton invariant mass distribution further allow for a determination of the mass difference of the heavy neutralino with the LSP.

In these scenarios the squarks are heavy so the gluino decays only via 3-body,  $\tilde{g} \rightarrow \tilde{\chi}_i^0 f \bar{f}$  or  $\tilde{g} \rightarrow \tilde{\chi}_i^0 f \bar{f}$  leading to final states with many jets as well as missing energy from the LSP. The branching fraction into third generation quarks is particularly relevant since it has been shown [50, 51] that requiring tagged b-quark jets in the final state helped reduce the SM background and thus could extend the LHC reach in this channel. In our sample scenarios, the total branching fraction for 3-body decays of gluinos into third generation quarks (t and b)  $B(\tilde{g} \rightarrow \chi Q Q') = B_{gQQ}$  varies over a wide range, from 0.1-0.8 and features two peaks around 25% and 70%, see figure 9a.<sup>5</sup> The  $\tilde{\chi}_2^0, \tilde{\chi}_3^0$  channels each contribute below 20%, see figure 9b. The larger branching fractions  $B_{gQQ}$  are found for low values of  $\mu$ , see figure 10, this is mainly because in this case all charginos and neutralinos can be produced in gluino decays and contribute significantly (especially charginos). The branching fraction  $B_{gQQ}$  also increases with tan  $\beta$ , this is because of the enhanced coupling of the higgsino to  $\tilde{b}b$ .

Next we have computed the decay modes of the  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_3^0$ . The  $\tilde{\chi}_2^0$  decays dominantly via 3-body, the branching fraction of neutralinos into each fermion pair is typical of the Z decay (around 3% for each leptonic mode), see figure 11. In some scenarios the two-body leptonic channels are accessible, in this case the  $\tilde{\chi}_2^0$  either decays exclusively into the lighest slepton (the stau) or into all sleptons including the invisible mode into sneutrinos, see figure 11b. Finally the decay channels into a gauge or Higgs boson and the LSP dominate for sufficient mass splitting between the neutralinos, the dominant mode is  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 h$ unless only the Z is kinematically accessible. For  $\tilde{\chi}_3^0$  a larger fraction of scenarios have 2-body decay modes, in particular the decays into neutral and charged gauge bosons,  $\tilde{\chi}_3^0 \to \tilde{\chi}_1^0 Z$ ,  $\mathrm{or} \tilde{\chi}_1^+ W$ . Decays into sleptons are as before confined to the scenarios with light sleptons, figure 12.

 $<sup>{}^{5}</sup>$ For reference recall that in a typical focus point scenario the branching ratios of gluinos into third generation quarks reach 72% [52].



**Figure 10**.  $B_{gQQ}$  as a function of  $\mu$  parameter.



**Figure 11.** Distribution of  $\tilde{\chi}_2^0$  branching fractions for the channels a)  $\tilde{\chi}_1^0 e^+ e^-(\mu^+\mu^-)$  b)  $\tilde{l}l$  c)  $\tilde{\chi}_1^0 Z, \tilde{\chi}_1^0 h$ . There is a scale factor of 10<sup>6</sup> on the y-axis.



**Figure 12.** a) Distribution of  $\tilde{\chi}_3^0$  branching fractions for the channels a)  $\tilde{\chi}_i^0 e^+ e^-, \mu^+ \mu^-$  b)  $\tilde{l}l$  c)  $\tilde{\chi}_1^0 Z, \tilde{\chi}_1^0 h, \tilde{\chi}_1^+ W$ . There is a scale factor of 10<sup>6</sup> on the y-axis.

Finally we have compiled the fraction of models (among set B only) that feature each dominant decay mode, the results are presented in table 8. The largest sample (35%) corresponds to both neutralinos decaying into 3-body channels. In these scenarios  $\mu <$ 

$ ilde{\chi}_2^0$	$ ilde{\chi}^0_3$	Fraction of models
$\tilde{\chi}_1^0 f \bar{f}$	$ ilde{\chi}^0_i f ar{f}$	35.2%
	$\chi_1^{\pm}W^{\mp}$	4.2%
$\tilde{\chi}_1^0 f \bar{f}$	$\chi_i Z, \chi_i h$	8.6%
	Ĩl	0.2%
$\tilde{\chi}_1^0 Z$	$\chi_1^{\pm}W^{\mp}$	6.0%
$\tilde{\chi}_1^0 h$	$\chi_i Z$ (or $\chi_1^{\pm} W^{\mp}$ )	14.4%
Ĩl	Ĩl	4.6%
	$\chi_1^{\pm}W^{\mp}$	6.1%
$\tilde{\chi}_1^0 f \bar{f}$	-	3.8%
$\tilde{\chi}_1^0 Z$	-	2.8%
$ ilde{\chi}_1^0 h$	-	6.7%
Ĩl	-	5.0%

**Table 8**. Dominant decay mode of  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_3^0$  in models with  $m_{\tilde{g}} < 2 \text{ TeV}$  and  $M_{\tilde{q}} > 2 \text{ TeV}$  and fraction of allowed models corresponding to each dominant decay mode.

350 GeV,  $\mu - M_1$  is small and the LSP has a significant higgsino component so that the direct detection rate is large ( $\sigma_{\chi p}^{SI} > 7 \times 10^{-9}$  pb). The scenarios where  $\tilde{\chi}_3^0$  instead has 2-body decays also have in general a LSP with an important higgsino component and a large  $\sigma_{\chi p}^{SI}$  except when  $\tilde{\chi}_3^0 \to \tilde{\chi}_1^+ W^-$  is the dominant channel. Then we found predominantly  $m_{\tilde{\chi}_1^0} \approx 60 \text{ GeV}$  with a bino LSP annihilating efficiently through a light Higgs resonance.

A large number of scenarios (31% of set B) correspond to both  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_3^0$  having 2-body decay modes. The case where the dominant decay mode is  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 Z$  correspond to a small value for  $\mu - M_1$ , this means a dominantly higgsino LSP. In general though the dominant modes are  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 h$  and  $\tilde{\chi}_3^0 \to \tilde{\chi}_1^0 Z$  unless sleptons are light. In nearly 19% of scenarios B,  $\mu$  is large and the  $\tilde{\chi}_3^0$  which is higgsino cannot be produced in gluino decays. The  $\tilde{\chi}_2^0$  decays predominantly via 2-body channels,  $\tilde{l}l, \chi_1 h$  or  $\chi_1 Z$  or into 3-body  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 f \bar{f}$  with the leptonic mode offering a robust signature. Typically in these scenarios the elastic scattering cross sections is small apart from the cases where the heavy Higgs is light enough to contribute significantly.

In conclusion, although the focus point like scenario where gluinos decay with large fraction into b quarks and leptonic 3 body decays of  $\tilde{\chi}_2^0, \tilde{\chi}_3^0$  constitute the largest sample, the channels with two body decays of neutralinos are also very important. Among these cases where leptonic decays of  $\tilde{\chi}_2^0$  dominate constitute 16% of our sample while those where the only final states include Z(W) or h constitute about 30% of our sample. Note that the gluino only scenario could be quite challenging for the LHC especially if the gluino is near 2TeV. We have checked that the scenarios that would be accessible with a lower luminosity, say  $m_{\tilde{g}} < 900 \text{ GeV}$  for  $\mathcal{L} = 30 \text{ fb}^{-1}$ , share the main features we have just described. Obviously because of the lighter spectrum a smaller fraction of scenarios have  $\tilde{\chi}_3^0$  accessible in gluinos decays. Furthermore the fraction of scenarios with 2-body decays is smaller with for example hardly any scenario where both  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_3^0$  decay via 2-body.

		bino	mixed	higgsino
		$f_H \le 0.01$	$0.01 < f_H \le 0.5$	$f_{H} > 0.5$
$\tilde{u}_L \to \tilde{\chi}_1^0 \ u$		7.7%	2.5%	—
$\tilde{u}_L \to \tilde{\chi}_3^0 \ u$	$\tilde{\chi}^0_3 \to \tilde{l} l$	-	-	0.3%
	$\tilde{\chi}_3^0 \to \tilde{\chi}_1^+ W$	-	-	0.3%
	$\tilde{\chi}_3^0 \to \tilde{\chi}_1^+ f' \bar{f}$	-	2.0%	7.4%
$\tilde{u}_L \to \tilde{\chi}_1^+ d$	$\tilde{\chi}_1^+ \to \tilde{\chi}_1^0 W$	12.4%	-	-
	$\tilde{\chi}_1^+ \to \tilde{l} l'$	8.9%	-	-
$\tilde{u}_L \to \tilde{\chi}_2^+ d$	$\tilde{\chi}_2^+ \to \tilde{\chi}_i^0 W$	2.7%	37.2%	2.5%
	$\tilde{\chi}_2^+ \to \tilde{\chi}_1^+ h$	-	1.0%	0.6%
	$\tilde{\chi}_2^+ \to \tilde{l} l'$	1.1%	12.5%	0.6%
Fraction of sample		32.8%	55.3%	11.9%

**Table 9.** Dominant decay chains for  $\tilde{u}_L$  for a bino, mixed or higsino LSP.

## 5.2 Scenarios where $M_{\tilde{q}} < 2$ TeV, $m_{\tilde{q}} > 2$ TeV

In the MSSM-UG a small fraction of allowed scenarios (set D) predicts that only squarks are lighter than 2TeV. In this case, the main contribution to SUSY production is direct production of squark pairs. In the MSSM-UG, the masses of sleptons and squarks are not correlated, so sleptons are not always light enough to be produced in neutralino decays. The conventional SUSY searches which involve a decay chain with a neutralino  $\tilde{q} \to \tilde{\chi}_2^0 j \to \tilde{l} l j \to \tilde{\chi}_1^0 \tilde{l} l j$  will be superseded by the two-body decays,  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 Z, \tilde{\chi}_1^0 h$  or  $\tilde{\chi}_1^+ W$  or if kinematically forbidden by 3-body decays.

We have computed the branching fractions for squarks, taking as an example the  $\tilde{u}_L$ and  $\tilde{u}_R$ . We have then looked for the dominant mode into either a chargino, a heavy neutralino or the direct decay into the LSP. In each case we have also examined the decay mode of the neutralinos and charginos that occur in squark decays. The higgsino fraction of the LSP is an important factor that determines the dominant decay mode. We therefore analyse the dominant decay modes separately for the case of a bino, mixed or higgsino LSP. Note that a mixed LSP constitutes more than half of our sample of scenarios.

The right-handed squark decays mainly into the bino component which means that the dominant decay is in general  $\tilde{u}_R \to u \tilde{\chi}_1^0$ , leading to only jets and missing energy. The decay  $\tilde{u}_R \to u \tilde{\chi}_3^0$  can occur only when the LSP is a higgsino  $(f_H \gtrsim 50\%)$  so that the  $\tilde{\chi}_1^0$ channel is suppressed. In this case however the heavier neutralino decays mostly via 3 body decays into the lightest chargino or neutralino + jets leading again to signatures with jets and missing energy.

The left-handed quark which couples strongly to the wino and/or higgsino component has a wide variety of decay modes. The frequency of each dominant decay chain are displayed in table 9 for each LSP configuration. For the bino LSP the dominant mode is usually  $\tilde{u}_L \to d\tilde{\chi}_1^+$  with typical branching fractions around 60%. The chargino will decay either into  $\tilde{\chi}_1^0 W$  or  $\tilde{l}l'$  when light sleptons are present. The subdominant mode in those scenario is  $\tilde{u}_L \to u\tilde{\chi}_2^0$  with  $\tilde{\chi}_2^0 \to \tilde{l}l, \tilde{\chi}_1^0 Z, \tilde{\chi}_1^0 h$ . The decay chains are similar to those of the CMSSM. In some cases the second chargino, a mixed higgsino/wino, is kinematically accessible and the dominant mode will be  $\tilde{u}_L \to d\tilde{\chi}_2^+$  with subdominant decays into  $\tilde{\chi}_4^0 u$ and  $\tilde{\chi}_1^+ d$ .  $\tilde{\chi}_2^+$  will decay preferentially into  $\tilde{\chi}_2^0 W$  or in other neutralinos as well as into  $\tilde{l}l$ . The Higgs can be produced in either  $\tilde{\chi}_2^+ \to \tilde{\chi}_1^+ h$  or further in  $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 h$ . A fraction of models (7.7%) feature the dominant decay into the LSP  $\tilde{u}_L \to u\tilde{\chi}_1^0$ . Because the squark  $\tilde{q}_L$  has a suppressed rate to the bino, this channel is dominant only when other two-body channels are kinematically forbidden.

For a mixed LSP (0.01 <  $f_H \leq 0.5$ ) the relative importance of the various decay channels shift. The decay  $\tilde{u}_L \to u \tilde{\chi}_1^0$  is dominant in less than 3% of the cases although because of the higgsino component of the LSP this can occur even when heavier neutralinos are kinematically accesssible. By far the most frequent dominant decay is  $\tilde{u}_L \to d \tilde{\chi}_2^+$  with significant branching fractions in  $u \tilde{\chi}_3^0$  or  $d \tilde{\chi}_1^+$ . The heavier chargino always has two-body decay modes,  $\tilde{\chi}_2^+ \to \tilde{\chi}_i^0 W$  (preferably  $\tilde{\chi}_2^0 W$ ) or  $\tilde{\chi}_2^+ \to \tilde{\chi}_1^+ h$ . The  $\tilde{\chi}_2^0, \tilde{\chi}_3^0$  and  $\tilde{\chi}_1^+$  in turn feature mostly 3-body decays. Note that decay modes into Higgs bosons  $\tilde{\chi}_2^+ \to \tilde{\chi}_1^+ h$  can involve even the heavy Higgs bosons. As usual when light sleptons are present the decay  $\tilde{\chi}_2^+ \to \tilde{l}l'$  can be dominant.

For the higgsino LSP  $(f_H > 0.5)$ , the dominant mode is either  $\tilde{\chi}_3^0 u$  or  $\tilde{\chi}_2^+ d$  with some contributions from  $\tilde{\chi}_2^+ d$  and  $\tilde{\chi}_4^0 u$ . The  $\tilde{\chi}_2^+$  channel has similar decay chains as the mixed LSP except that the dominant mode is usually  $\tilde{\chi}_2^+ \to \tilde{\chi}_2^0 W$  rather than channels involving Higgses. The  $\tilde{\chi}_3^0$  can in a few cases decay via two-body,  $\tilde{\chi}_1^+ W$  or  $\tilde{l}l$ , but in most cases it decays via three-body dominantly into  $\tilde{\chi}_3^0 \to \tilde{\chi}_1^+ f f'$ . These decays mainly give signatures into jets and missing energy. The  $\tilde{\chi}_1^+$  produced in squark or neutralino decays will also decay via three body final states.

In summary  $\tilde{q}_L$  decays dominantly into heavy charginos with further decay chains involving other chargino/neutralino states. Decay chains involving slepton production dominater only in 25% of scenarios. Finally recall that the elastic scattering cross section also differs significantly depending on the nature of the LSP giving an opportunity to correlate SUSY signals at LHC with those of direct detection. For the bino LSP,  $\sigma_{\chi p}^{SI} < 10^{-9}$  pb while  $\sigma_{\chi p}^{SI} > 10^{-9} (5 \times 10^{-8})$  pb for the mixed (higgsino) LSP.

## 5.3 Scenarios where $M_{\tilde{q}} < 2$ TeV, $m_{\tilde{q}} < 2$ TeV

We finally briefly summarise the results for the case where both squarks and gluinos are lighter than 2 TeV, recall that 15.5% of the allowed scenarios fall within this category. In 80% of this sample, the gluino is the lightest sparticle. The squarks decay dominantly into gluinos and quarks or into heavier neutralinos/charginos while the decay modes of the gluino resemble the ones discussed in section 5.1 although the decay chains involving only 3-body decays are more likely. Specifically, in 75% of the scenarios the gluino will dominantly decay into  $\tilde{\chi}_i^0 \bar{f} f, \tilde{\chi}_i^+ \bar{f} f'$  and the heavy neutralinos will in turn have dominantly 3-body decay modes. When 2-body modes of the heavy neutralinos are kinematically open, it is the production of a gauge boson and/or of a Higgs that is favoured.

For the cases where the squarks are lighter than gluinos (more precisely here it means the  $\tilde{u}_L, \tilde{u}_R$ ), the gluino decay into squark/quark pairs. The right-handed quark as usual decay into a quark and a LSP while the left-handed quark decay predominantly into charginos. If the LSP is a bino the favoured decay chain is  $\tilde{u}_L \to \tilde{\chi}_1^+ d, \tilde{\chi}_1^+ \to \tilde{\chi}_1^0 W$  while for the mixed higgsino LSP the favoured chain involves rather the heavy chargino,  $\tilde{\chi}_2^+$ . In contrast with the case where only squarks are lighter than 2 TeV, see section 5.2, the decay chains with slepton production are never dominant. Furthermore the LSP is either bino or mixed but never dominantly higgsino.

## 6 Conclusion

Increasing the number of free parameters as compared to the CMSSM model has opened up the possibilities for supersymmetric scenarios that are compatible with all experimental constraints and this even while maintaining the universality of gaugino masses. Although the parameter space of the model is still not very well constrained, we found that the most favoured models have a LSP of a few hundred GeV with a significant higgsino fraction (> 10%). Contrary to the CMSSM case the higgsino LSP is not fully correlated with a very heavy squark sector although all our scenarios favour squarks near or above the TeV scale. A very light pseudoscalar is also disfavoured with  $M_A > 340 \,\text{GeV}$ , this means that large deviations from the SM in B-physics observables are expected only in a small fraction of allowed scenarios. This is especially so when using log priors. Our favoured scenarios predict few signals at the Tevatron, the pseudoscalar Higgs as well as the coloured sector are too heavy to be accessed by direct searches. Only very few scenarios have a potentially large enough rate for trilepton searches at the Tevatron. The complementarity between future experiments to probe this class of models was emphasized. Even though SUSY or heavy Higgs signals are not guaranteed at LHC, the majority of allowed models predict at least one signal either at the LHC (including the flavour sector) or in future direct detection experiment. Furthermore the light Higgs is expected to be around 120GeV with SM-like couplings.

We have also explored the various dominant decay chains for gluinos and squarks that could be produced at LHC in the MSSM-UG as well as for the heavy neutralinos appearing in the decays of these coloured sparticles for the fit with linear priors. We found that for models with gluinos accessible at LHC, a significant fraction of the heavy neutralinos produced decayed dominantly into a gauge or Higgs boson. Furthermore states which decayed into sleptons are rarely dominant. We also showed how the preferred squarks decay channels are determined to a large extent by the neutralino composition. Whether one can exploit these decay chains to determine some properties of the sparticles remains to be seen. In our analysis the relic density measurement plays the dominant role in constraining the model. Since the relic density computation implicitly assumes a standard cosmological scenario, relaxing this requirement would affect significantly the allowed parameter space of the model.

Finally we comment on the difference between our results and other recent analyses done within the framework of the MSSM with 24 parameters, either using a MCMC likelihood approach [27] or applying  $2\sigma$  constraints on each of the observables [26, 53]. First these studies were done in a more general model than the one we have considered, with in particular no universality condition on the gaugino masses. This means that the LSP can have a significant wino component and therefore is more likely to be at the TeV scale as was found in [27] using linear priors. Recall that a TeV scale wino annihilates efficiently into gauge bosons pairs. The analysis of [27] also emphasizes the prior dependence with a generally much lighter spectrum using log priors. This is due mostly to the poorly constrained parameter space [54, 55]. As in our analysis squarks and sleptons ran over the full range allowed in the scan and the pseudoscalar mass can be very heavy.

The analysis of [26] used a different statistical treatment but most importantly did not require that the neutalino explained all the DM in the universe (only an upper bound on  $\Omega h^2$  was imposed). This means that a large number of models with small mass splitting between the LSP and the NLSP appeared in the scan calling for a careful study of collider limits. In our approach such models are ruled out since they have  $\Omega h^2 \ll 0.1$ . This analysis further emphasized the light SUSY spectrum in their scans so naturally found preferred LSP mass below the TeV scale.

## Acknowledgments

We thank J. Hamann for many useful discussions on the MCMC method. We acknowledge support from the Indo French Center for Promotion of Advanced Scientific Research under project number 30004-2. This work was also supported in part by the GDRI-ACPP of CNRS and by the French ANR project ToolsDMColl, BLAN07-2-194882. The work of A.P. was supported by the Russian foundation for Basic Research, grant RFBR-08-02-00856-a and RFBR-08-02-92499-a. The work of R.K.S. is supported by the German BMBF under contract 05HT6WWA

## References

- XENON collaboration, J. Angle et al., First Results from the XENON10 Dark Matter Experiment at the Gran Sasso National Laboratory, Phys. Rev. Lett. 100 (2008) 021303
   [arXiv:0706.0039] [SPIRES].
- [2] CDMS collaboration, Z. Ahmed et al., Search for Weakly Interacting Massive Particles with the First Five-Tower Data from the Cryogenic Dark Matter Search at the Soudan Underground Laboratory, Phys. Rev. Lett. 102 (2009) 011301 [arXiv:0802.3530] [SPIRES].
- [3] PAMELA collaboration, O. Adriani et al., An anomalous positron abundance in cosmic rays with energies 1.5.100 GeV, Nature 458 (2009) 607 [arXiv:0810.4995] [SPIRES].
- [4] THEFERMI LAT collaboration, A.A. Abdo et al., Measurement of the Cosmic Ray e+ plus e- spectrum from 20 GeV to 1 TeV with theFermi Large Area Telescope, Phys. Rev. Lett. 102 (2009) 181101 [arXiv:0905.0025] [SPIRES].
- [5] H.E.S.S. collaboration, F. Aharonian et al., The energy spectrum of cosmic-ray electrons at TeV energies, Phys. Rev. Lett. 101 (2008) 261104 [arXiv:0811.3894] [SPIRES].
- [6] O. Adriani et al., A new measurement of the antiproton-to-proton flux ratio up to 100 GeV in the cosmic radiation, Phys. Rev. Lett. 102 (2009) 051101 [arXiv:0810.4994] [SPIRES].
- [7] WMAP collaboration, E. Komatsu et al., Five-Year Wilkinson Microwave Anisotropy Probe (WMAP) Observations: Cosmological Interpretation, Astrophys. J. Suppl. 180 (2009) 330
   [arXiv:0803.0547] [SPIRES].

- [8] WMAP collaboration, D.N. Spergel et al., Wilkinson Microwave Anisotropy Probe (WMAP) three year results: Implications for cosmology, Astrophys. J. Suppl. 170 (2007) 377
   [astro-ph/0603449] [SPIRES].
- [9] SDSS collaboration, M. Tegmark et al., Cosmological Constraints from the SDSS Luminous Red Galaxies, Phys. Rev. D 74 (2006) 123507 [astro-ph/0608632] [SPIRES].
- [10] CDF collaboration, T. Aaltonen et al., Search for new physics in the  $\mu\mu + e/\mu + E_T$  channel with a low- $p_T$  lepton threshold at the Collider Detector at Fermilab, *Phys. Rev.* D 79 (2009) 052004 [arXiv:0810.3522] [SPIRES].
- [11] D0 collaboration, V.M. Abazov et al., Search for associated production of charginos and neutralinos in the trilepton final state using 2.3 fb-1 of data, Phys. Lett. B 680 (2009) 34
   [arXiv:0901.0646] [SPIRES].
- [12] E. Aprile, L. Baudis and f.t.X. Collaboration, Status and Sensitivity Projections for the XENON100 Dark Matter Experiment, arXiv:0902.4253 [SPIRES].
- [13] CDMS collaboration, T. Bruch, Status and future of the CDMS experiment: CDMS-II to SuperCDMS, AIP Conf. Proc. 957 (2007) 193 [SPIRES].
- [14] GLAST LAT collaboration, A.A. Moiseev, Gamma-ray Large Area Space Telescope: Mission overview, Nucl. Instrum. Meth. A 588 (2008) 41 [SPIRES].
- [15] E. Mocchiutti et al., The PAMELA Space Experiment, arXiv:0905.2551 [SPIRES].
- [16] ATLAS collaboration, ATLAS detector and physics performance. Technical design report. Vol. 2, CERN-LHCC-99-015 [SPIRES].
- [17] CMS collaboration, G.L. Bayatian et al., CMS technical design report, volume II: Physics performance, J. Phys. G 34 (2007) 995 [SPIRES].
- [18] M. Artuso et al., B, D and K decays, Eur. Phys. J. C 57 (2008) 309 [arXiv:0801.1833] [SPIRES].
- [19] J.R. Ellis, S. Heinemeyer, K.A. Olive, A.M. Weber and G. Weiglein, The Supersymmetric Parameter Space in Light of B<sup>-</sup> physics Observables and Electroweak Precision Data, JHEP 08 (2007) 083 [arXiv:0706.0652] [SPIRES].
- [20] H. Baer and C. Balázs,  $Chi^2$  analysis of the minimal supergravity model including WMAP, g(mu)-2 and  $b \rightarrow s\gamma$  constraints, JCAP **05** (2003) 006 [hep-ph/0303114] [SPIRES].
- [21] G. Bélanger, F. Boudjema, A. Cottrant, A. Pukhov and A. Semenov, WMAP constraints on SUGRA models with non-universal gaugino masses and prospects for direct detection, Nucl. Phys. B 706 (2005) 411 [hep-ph/0407218] [SPIRES].
- [22] E.A. Baltz and P. Gondolo, Markov chain Monte Carlo exploration of minimal supergravity with implications for dark matter, JHEP 10 (2004) 052 [hep-ph/0407039] [SPIRES].
- [23] B.C. Allanach and C.G. Lester, Multi-Dimensional mSUGRA Likelihood Maps, Phys. Rev. D 73 (2006) 015013 [hep-ph/0507283] [SPIRES].
- [24] B.C. Allanach, C.G. Lester and A.M. Weber, *The Dark Side of mSUGRA*, *JHEP* **12** (2006) 065 [hep-ph/0609295] [SPIRES].
- [25] R.R. de Austri, R. Trotta and L. Roszkowski, A Markov chain Monte Carlo analysis of the CMSSM, JHEP 05 (2006) 002 [hep-ph/0602028] [SPIRES].

- [26] C.F. Berger, J.S. Gainer, J.L. Hewett and T.G. Rizzo, Supersymmetry Without Prejudice, JHEP 02 (2009) 023 [arXiv:0812.0980] [SPIRES].
- [27] S.S. AbdusSalam, B.C. Allanach, F. Quevedo, F. Feroz and M. Hobson, *Fitting the Phenomenological MSSM*, arXiv:0904.2548 [SPIRES].
- [28] H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, Direct, indirect and collider detection of neutralino dark matter in SUSY models with non-universal Higgs masses, JHEP 07 (2005) 065 [hep-ph/0504001] [SPIRES].
- [29] A. Bottino, F. Donato, N. Fornengo and S. Scopel, Size of the neutralino nucleon cross-section in the light of a new determination of the pion nucleon sigma term, Astropart. Phys. 18 (2002) 205 [hep-ph/0111229] [SPIRES].
- [30] G. Bélanger, F. Boudjema, A. Pukhov and A. Semenov, Dark matter direct detection rate in a generic model with MicrOMEGAs2.1, Comput. Phys. Commun. 180 (2009) 747 [arXiv:0803.2360] [SPIRES].
- [31] G. Bélanger et al. in preparation.
- [32] Z. Zhang, Muon g-2: a mini review, arXiv:0801.4905 [SPIRES].
- [33] D. Mackay, Information theory, Inference, and learning Algorithms, Cambridge University Press, Cambridge U.K. (2003).
- [34] HEAVY FLAVOR AVERAGING GROUP (HFAG) collaboration, E. Barberio et al., Averages of b-hadron properties at the end of 2006, arXiv:0704.3575 [SPIRES].
- [35] A. Sanchez-Hernandez, Tevatron results on b-hadron lifetimes and rare decays, Proceedings of 42nd Rencontres de Moriond, La Thuile, March 10–17, 2007.
- [36] HEAVY FLAVOR AVERAGING GROUP collaboration, E. Barberio et al., Averages of b-hadron and c-hadron Properties at the End of 2007, arXiv:0808.1297 [SPIRES].
- [37] LEP WORKING GROUP FOR HIGGS BOSON SEARCHES collaboration, R. Barate et al., Search for the standard model Higgs boson at LEP, Phys. Lett. B 565 (2003) 61
   [hep-ex/0306033] [SPIRES].
- [38] PARTICLE DATA GROUP collaboration, C. Amsler et al., Review of particle physics, Phys. Lett. B 667 (2008) 1 [SPIRES].
- [39] A. Gelman and D. Rubin, Inference From Iterative Simulation Using Multiple Sequences, Stat. Sci. 7 (1992) 457.
- [40] B.C. Allanach, SOFTSUSY: A C++ program for calculating supersymmetric spectra, Comput. Phys. Commun. 143 (2002) 305 [hep-ph/0104145] [SPIRES].
- [41] G. Bélanger, F. Boudjema, A. Pukhov and A. Semenov, *MicrOMEGAs: Version 1.3*, *Comput. Phys. Commun.* **174** (2006) 577 [hep-ph/0405253] [SPIRES].
- [42] G. Bélanger, F. Boudjema, A. Pukhov and A. Semenov, MicrOMEGAs2.0: A program to calculate the relic density of dark matter in a generic model, Comput. Phys. Commun. 176 (2007) 367 [hep-ph/0607059] [SPIRES].
- [43] M. Misiak et al., The first estimate of  $B(anti-B \rightarrow X/s \ gamma)$  at  $O(\alpha_s^2)$ , Phys. Rev. Lett. **98** (2007) 022002 [hep-ph/0609232] [SPIRES].
- [44] CDF collaboration, T. Aaltonen et al., Search for  $B_s^0 \to \mu^+\mu^-$  and  $B_d^0 \to \mu^+\mu^-$  decays with  $2fb^{-1}$  of  $p\bar{p}$  collisions, Phys. Rev. Lett. **100** (2008) 101802 [arXiv:0712.1708] [SPIRES].

- [45] D0 collaboration, V.M. Abazov et al., Search for squarks and gluinos in events with jets and missing transverse energy using 2.1  $fb^{-1}$  of  $p\bar{p}$  collision data at  $\sqrt{s} = 1.96 \text{ TeV}$ , Phys. Lett. **B 660** (2008) 449 [arXiv:0712.3805] [SPIRES].
- [46] M. Davier, g-2, Talk presented at Tau'08, Novosibirsk, Russia.
- [47] A. Dedes, H.K. Dreiner and U. Nierste, Correlation of  $B_s \to \mu^+ \mu^-$  and (g-2) ( $\mu$ ) in minimal supergravity, Phys. Rev. Lett. 87 (2001) 251804 [hep-ph/0108037] [SPIRES].
- [48] J. Lewis, B Physics Results from the Tevatron: Lifetimes and Rare Decays, talk presented at Moriond electrowek 2009, LaThuile, Italy, March 2009.
- [49] A. Dedes, H.K. Dreiner, U. Nierste and P. Richardson, *Trilepton events and*  $B_s \rightarrow \mu^+ \mu^-$ : No lose for mSUGRA at the Tevatron?, hep-ph/0207026 [SPIRES].
- [50] P.G. Mercadante, J.K. Mizukoshi and X. Tata, Using b-tagging to enhance the SUSY reach of the CERN Large Hadron Collider, Phys. Rev. D 72 (2005) 035009 [hep-ph/0506142] [SPIRES].
- [51] R.H.K. Kadala, P.G. Mercadante, J.K. Mizukoshi and X. Tata, *Heavy-flavour tagging and the supersymmetry reach of the CERN Large Hadron Collider*, *Eur. Phys. J.* C 56 (2008) 511 [arXiv:0803.0001] [SPIRES].
- [52] U. De Sanctis, T. Lari, S. Montesano and C. Troncon, Perspectives for the detection and measurement of Supersymmetry in the focus point region of mSUGRA models with the ATLAS detector at LHC, Eur. Phys. J. C 52 (2007) 743 [arXiv:0704.2515] [SPIRES].
- [53] S. Profumo and C.E. Yaguna, A statistical analysis of supersymmetric dark matter in the MSSM after WMAP, Phys. Rev. D 70 (2004) 095004 [hep-ph/0407036] [SPIRES].
- [54] B.C. Allanach, K. Cranmer, C.G. Lester and A.M. Weber, Natural Priors, CMSSM Fits and LHC Weather Forecasts, JHEP 08 (2007) 023 [arXiv:0705.0487] [SPIRES].
- [55] R. Trotta, F. Feroz, M.P. Hobson, L. Roszkowski and R. Ruiz de Austri, The Impact of priors and observables on parameter inferences in the Constrained MSSM, JHEP 12 (2008) 024 [arXiv:0809.3792] [SPIRES].